Sunday 5 ${ }^{\text {th }}$ February, 2023

## Problem Caesar Is Back

C header caesar.h<br>C++ header caesar.h

Your favourite emperor CAESAR is back! He gives you the following problem. He defines a 1-step transformation in the following way: a 1-step transformation transforms an 'a' into a ' $b$ ', $a$ ' b' into $a^{\prime} c$ ', ..., $a^{\prime} y$ ' into $a^{\prime} z$ ', and finally $a$ ' $z$ ' into an ' $a$ '. Furthermore, for any non-negative integer $k$, he defines a $k$-step transformation as a 1 -step transformation applied $k$ times. For example, a 3 -step transformation transforms an ' $a$ ' into a 'd'. Note that a 0 -step transformation does nothing i.e. it transforms an ' $a$ ' into an ' $a$ ', $a$ ' $b$ ' into $a$ ' $b$ ', and so on.

CaEsAR provides you with two strings $A$ and $B$, each of length $n$. These are both indexed from 0. Furthermore, he provides you with $q$ intervals $[l, r]$ where $0 \leq l \leq r<n$. For each interval $[l, r]$, he wants you to find the number of pairs $(x, y)$ such that $l \leq x \leq y \leq r$ and there exists a $k$ such that, for all $x \leq i \leq y$, we have that $B_{i}$ is the $k$-step transformation of $A_{i}$.

For example, if $n=3, A=\mathrm{aac}, B=\mathrm{bbc}, l=0$ and $r=2$ then the valid pairs are $(0,0),(0,1),(1,1)$ and $(2,2)$. For $(0,0),(0,1),(1,1)$ we take $k=1$, and for $(2,2)$ we take $k=0$.

## Interaction Protocol

The contestant must implement two functions:

```
void init(int n, int q, char A[], char B[]);
long long query(int l, int r);
```

The function init will be called exactly once, at the beginning of the interaction. The function will be supplied with the values $n$ and $q$ and with the two strings, $A$ and $B$. Then, the committee will call the function query $q$ times. It will be supplied with the values $l$ and $r$, representing a query. The contestant must return one integer, the answer for the interval $[l, r]$, according to the statement.

Attention! The contestant must not implement the main function, and must \#include the caesar.h header! Contestants are allowed to use global variables and other functions.

## Restrictions

- $1 \leq n \leq 1000000$.
- $1 \leq q \leq 1000000$.
- $A$ and $B$ contain lowercase English letters only.

| $\#$ | Points | Restrictions |
| :---: | :---: | :--- |
| 1 | 5 | $A=$ aaa..,$B=\mathrm{bbb} \ldots$ |
| 2 | 9 | $A$ and $B$ contain only ' a ' and ' n ' |
| 3 | 10 | $n \leq 100, q \leq 1000$ |
| 4 | 15 | $n \leq 1000, q \leq 300000$ |
| 5 | 30 | $q \leq 100000$ |
| 6 | 31 | No further restrictions |

## Examples

| Input | Output |
| :---: | :---: |
| $\begin{aligned} & \text { init(3, 1, "aac", "bbc") } \\ & \text { query }(0,2) \end{aligned}$ | 4 |
| ```init(5, 3, "abcde", "bcdyz") query(1, 3) query(0, 2) query(4, 4)``` | $\begin{aligned} & 4 \\ & 6 \\ & 1 \end{aligned}$ |
| ```init(20, 20, "aggccdaloaxgnakfivqd", "ckjdfgdnsczhpdmilxrh") query(2, 9) query(8, 10) query(2, 11) query(3, 4) query(9, 15) query(6, 12) query(8, 10) query(8, 10) query(2, 5) query(5, 14) query(8, 13) query(5, 11) query(0, 1) query(6, 14) query(0, 5) query(2, 2) query(0, 3) query(9, 14) query(3, 12) query(8, 11)``` | 11 <br> 4 <br> 14 <br> 2 <br> 8 <br> 8 <br> 4 <br> 4 <br> 5 <br> 12 <br> 7 <br> 9 <br> 2 <br> 10 <br> 7 <br> 1 <br> 4 <br> 7 <br> 14 <br> 5 |

## Explanations

First example For the interval $[0,2]$ the valid pairs are $(0,0),(0,1),(1,1)$ and $(2,2)$. For the first three pairs we take $k=1$ which transforms the letters ' $a$ ' into letters ' $b$ '. For the last one we take $k=0$ which leaves the letter ' c ' as it is.

Second example For the interval $[1,3]$ we have the valid pairs $(1,1),(1,2)(2,2)$ and $(3,3)$. For $(1,1)$, $(1,2)$ and ( 2,2 ) we choose $k=1$ which transforms the letter ' $b$ ' into ' $c$ ' and the letter ' c ' into ' d ' respectively. For $(3,3)$ we choose $k=21$, because it transforms the letter ' $d$ ' into ' $y$ '. Therefore, the answer is 4 . For the interval $[0,2]$ every possible pair is valid. For all of them we choose $k=1$, which makes the letter ' $a$ ' into ' $b$ ', the letter ' $b$ ' into ' $c$ ' and the letter ' $c$ ' into ' $d$ ' respectively. Therefore, the answer is 6 . For the interval $[4,4]$ the only pair that satisfies the statement is $(4,4)$, for which we choose $k=21$, which transforms the letter ' e ' into ' z '. Therefore, the answer is 1 .

